# Use of Modern Computing Technique to Improve the Energy Indicators of Drive Motors of the Coal Mills

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Abstract - In this paper, the authors present a study on the energetic opportunity to replace derated motors of the five mills which are in service at a power plant with other motors by a rated power closer to the actual load. To this end, it has previously been drawn up a suggestive comparative analysis of diagrams of active and reactive power balance in absolute and percentage values for each case of considered constructive variants. Thus for drawing up, using the complete mathematical model (BEMAS) chosen for the asynchronous machine, of the electric balances for different operating regimes of these asynchronous motors, it was necessary to determine the parameters of the equivalent diagram. Considering the complexity and large volume of computation, the authors developed for this purpose, specific computational algorithms. For all these computational algorithms, computation programs have been drawn, being developed in the programming environment Mathcad Version 7.0, of own conception and which in principle can be used for any other similar motors that have different nominal data. It has also been highlighted that the starting point to establishing the opportunity of replacing of the analyzed asynchronous motors operating derated in steady state, is determining the actual load degree that is achieved through active power measurement for the considered regime.

**Keywords:** *electric balance, complete mathematic model, energy indicators, coal mills, power plant.* 

### I. INTRODUCTION

At the boiler with steam rated flow from the high pressure, 1035 t/h equipping a power plant, the coal is burned in powder form.

The preparation of the coal dust is made with six mills, combined with hammers and a fan. The six mills of the boiler and associated coal dust burners are placed so around the boiler that their axes are tangent to an imaginary circle with a diameter of 1500 mm with centre in the centre of the outbreak (swirling outbreak), Fig. 1.

The coal mills dry and mill the coal in a single operation after it has been crushed at the fuel household to a particle size of the 0 - 30 mm, with the maximum particle size 40 mm up to 15 %. The six mills are modernized mill type DGS-100. The mill DGS-100 is built in two versions: the right and left, the difference between these variants consisting of the sense of rotation of the fan rotor. The mill DGS-100 has the rated flow in an operation cycle of the hammers 100 t/h and is driven by an asynchronous motor having the following rated parameters:  $P_n = 1400$  kW,  $U_n = 6$  kV, synchronous speed  $n_s = 1500$  rot/min.

The fan mill (Fig. 2) with hammers is composed of a supply casing, the casing of the mill itself, the fan casing, the separator (1), the connection pipelines to the burners, a shaft hingeably provided with five rows of hammers and the fan mill and the mill drive (2). Above the supply casing flange is located the insulation shutter of the mill (3) with the gas pipeline and supply pipeline.

As it is shown in Fig. 3, the mill drive is composed of (M) the asynchronous electric motor - MIB-2A-630L-150-4, (CH) the hydraulic coupler - CHR 850 E-0 and (R) the speed reducer, with the transmission ratio i = 1:3.1.



Fig. 1. Arrangement of mills around the boiler and their numbering.



Fig. 2. View of the fan mill with hammers DGS-100.



Fig. 3. Electric drive of the mill DGS-100.

### II. THE ELECTRIC BALANCE OF THE ASYNCHRONOUS MOTOR TO DRIVE A COAL MILL USING THE COMPLETE MATHEMATIC MODEL

## *A.* Determination of parameters of the asynchronous motor to drive a DGS-100 coal mill

It is considered the squirrel cage asynchronous motor with high rectangular copper bars in two constructive variants Variant I and Variant II, having the catalogue data as in Table I.

TABLE I. The Technical Characteristics Of The Asynchronous Motor To Drive A Coal Mill

The technical characteristic	Variant I	Variant II	
name	MIB 2-Ax 630L	MIB-X 630L	
	150-4	150-4	
Rated power, $P_n$ [kW]	1400	1400	
Rated voltage, $U_n$ [kV]		6	
Rated current, $I_n$ [A]	155	156	
Rated speed, $n_n$ [rot/min]	1488	1492	
Power factor, $\cos \varphi_n$	0,91	0,91	
Efficiency, $\eta$ [%]	95,2	95,2	
Rated slip,	0.008	0.005333	
$s_n = (n_s - n_n) / n_s$			
Number of pole pairs, p		2	
Starting current, $i_p = I_p/I_n$	4,8	5,8	
reported to $U = U_n$			
Starting torque,	1,4	1,1	
$m_p = M_p/M_n$			
reported to $U = U_n$			
Maximum torque,	2,2	2,1	
$m_m = M_{max} / M_n$			
reported to $U = U_n$			
No load current, $I_0$ [A]	28,5	34	
Reduced height of the rotor	22.44		
bar, h			
Losses in the iron, $P_{Fe}$	32,375	3,5	
[kW]			



Fig. 4. Computation equivalent scheme for the asynchronous motor.

The parameters of the asynchronous machine equivalent scheme, which is shown in Figure 4, have been computed according to the following existing algorithms in the specialty literature [1], [2], [3].

$$U_{sn} = \frac{U_n}{\sqrt{3}}$$

$$I_w = \frac{1}{3} \frac{P_{Fe}}{U_{sn}}$$

$$R_w = \frac{U_{sn}}{I_w}$$
(1)

$$I_{sdn} = I_n \cos \varphi_n - I_w$$

$$I_{sm} = I_n \sin \varphi_n \qquad (2)$$

$$I_{sqn} = I_n \sin \varphi_n$$

$$I_{sn} = \sqrt{I_{sdn}^2 + I_{sqn}^2}$$
(2)

$$R_{abn} = \frac{U_{sn}I_{sdn}}{I_{sn}^2}; \quad X_{abn} = \frac{U_{sn}I_{sqn}}{I_{sn}^2}$$
(3)

$$A = 1 - 2s_n(m_m - 1); \quad B = 2m_m \tag{4}$$

$$s_m = s_n \frac{B + \sqrt{B^2 - 4A}}{2A} \tag{5}$$

$$a_{c} = \frac{1}{s_{m}^{2}}; \quad b_{c} = \frac{1 + s_{n}^{2}a_{c} - 2s_{n}m_{m}\sqrt{a_{c}}}{s_{n}(m_{m} - 1)}$$
(6)

$$a = \frac{2\sqrt{a_c}}{b_c}; \quad b = \frac{2}{s_n b_c}; \quad c = \frac{R_{abn}}{X_{abn}}$$
(7)

$$q = \frac{ac(a^2 + b^2) + 2b^2}{a^2b + b^2(1 + ac)}; \quad r = \frac{a^2 + b^2}{a^2b + b^2(1 + ac)}$$
(8)

$$\sigma = 0.5 \left( q + \sqrt{q^2 - 4r} \right) \tag{9}$$

$$m_s = \frac{1 - \sigma}{\sqrt{a^2 \sigma^2 - 1}}; \quad m_R = \frac{2m_s \sigma}{b_c} \tag{9'}$$

$$X_{s} = \frac{m_{R}^{2} + s_{n}^{2}}{m_{R}^{2} + s_{n}^{2}(1 - \sigma)} X_{abn}; \quad R_{s} = m_{s} X_{s}$$
(10)

$$X_{\mu} = \frac{X_s}{1.03}; \quad X_R' = \frac{X_{\mu}^2}{\sigma X_s}; \quad R_R' = m_R X_R'$$
(11)

$$X_s = X_{\sigma s} + X_{\mu} \tag{12}$$

$$X_{R} = X_{\sigma R} + X_{\mu}$$
$$X_{\sigma x} = X_{s} - X_{\mu}$$

$$X'_{\sigma R} = X'_R - X_\mu \tag{13}$$

For motors with high bars in the rotor in order to separate the components of resistance and the reactance of the rotor, the computation is continued by the following formulas:

$$K_{c} = \frac{1.5 p U_{sn}^{2}}{\omega R_{s}} b_{c}$$

$$M_{en} = \frac{s_{n} K_{c}}{s_{n}^{2} a_{c} + s_{n} b_{c} + 1}$$
(14)

$$R_{sc} = \frac{\omega m_p M_{en}}{3p i_p^2 I_n^2} + R_s$$

$$X_{sc} = \sqrt{\frac{U_{sn}^2}{i_p^2 I_n^2} - R_{sc}^2}$$
(15)

$$m_{Rsc} = \frac{R_{sc} - R_s}{X_s - X_{sc}}$$

$$\sigma_s = \frac{X_{\mu}}{X}$$
(16)

$$\sigma_{Bsc} = \frac{X_{sc} - m_{Rsc}(R_{sc} - R_s)}{X_s}$$
$$\sigma_{Rsc} = \frac{1 - \sigma_{Bsc}}{Z_s}$$

$$X'_{Rsc} = \frac{X_{\mu}}{\sigma_{Rsc}}$$
(17)

$$R'_{Rsc} = m_{Rsc} X'_{Rsc}$$

$$k_{Rsc} = h'$$

$$k_{Xsc} = \frac{1.5}{1}$$
(18)

$$R'_{RV} = \frac{R'_{Rsc} - R'_{R}}{k}$$

$$X'_{RV} = \frac{X'_{Rsc} - X'_{R}}{k_{Xsc} - 1}$$
(19)

$$\dot{R}_{RC} = R_{R}^{'} - \dot{R}_{RV}^{'}$$
  
 $\dot{X}_{RC} = X_{R}^{'} - X_{RV}^{'}$  (20)

 TABLE II.

 The Computed Parameters Of The Computation Equivalent

 Scheme For The Asynchronous Motor To Drive A Coal Mill

Parameter	Variant I Variant II		
	MIB 2-Ax 630L 150-4	MIB-X 630L 150-4	
$I_{\rm W}$ [A]	3.115	3.368	
$R_{\rm W}[\Omega]$	1112	1029	
$I_{sdn}[\mathbf{A}]$	137.935	138.592	
$I_{sqn}[\mathbf{A}]$	64.264	64.679	
$I_{sn}[\mathbf{A}]$	152.171	152.942	
$R_{abn} \left[ \Omega \right]$	20.635	20.525	
$X_{abn} \left[ \Omega \right]$	9.614	9.579	
$X_{s}[\Omega]$	106.317	113.489	
$R_s[\Omega]$	0.189	0.125	
$X_{\mu}[\Omega]$	103.22	110.184	
$X_{R}$ [ $\Omega$ ]	105.462	112.499	
$R_R$ [ $\Omega$ ]	0.178	0.118	
$X_{\sigma s} [\Omega]$	3.097	3.306	
$X_{\sigma R}$ [ $\Omega$ ]	2.242	2.316	
$R_{sc} \left[ \Omega \right]$	0.788	0.446	
$X_{sc} \left[ \Omega \right]$	4.589	3.803	
$X_{Rsc}$ [ $\Omega$ ]	104.731	110.682	
$R_{Rsc}[\Omega]$	0.616	0.323	
$R_{RV}$ [ $\Omega$ ]	0.02	0.009594	
$X_{RV}$ [ $\Omega$ ]	0.784	1.947	
$R_{RC}$ [ $\Omega$ ]	0.158	0.108	
$X_{RC}$ [ $\Omega$ ]	$\Gamma_{RC}[\Omega] = 104.678 = 110.552$		

These parameters are summarized in Table II, where:  $I_{\rm W}$  [A] - the corresponding current to the iron losses (oc-

curring in resistance  $R_W$ );  $R_{RV}$  [ $\Omega$ ] - the phase dispersion resistance corresponding to portions of the rotor winding comprised the inside of

the magnetic core of the rotor, reported to the stator;  $X_{RV}$  [ $\Omega$ ] - the phase dispersion reactance corresponding to portions of the rotor winding comprised the inside of the magnetic core of the rotor, reported to the stator;

 $R_{RC}$  [ $\Omega$ ] - the phase dispersion resistance corresponding to winding portions located outside of the rotor core (bar ends and shorting rings), reported to the stator;

 $X_{RC}$  [ $\Omega$ ] - the phase dispersion reactance corresponding to winding portions located outside of the rotor core (bar ends and shorting rings), reported to the stator. The computation of parameters of computing equivalent scheme was required to obtain then the main components of electric balance and energy indicators for the rated regime of asynchronous motor. The electric balance of active and reactive powers for the rated regime of the asynchronous motor to drive coal mill was then drawn up using a complete mathematic model (BEMAS) for the two constructive variants. The diagrams of active and reactive powers balance at the asynchronous motor, in absolute and percentage values have been represented for Variant I (Fig. 5, Fig. 7) and for Variant II (Fig. 6, Fig. 8). The energy indicators (efficiency and power factor) of the motors to drive coal mills have been also computed in the two constructive variants, the results being summarised in Table III. For all these computing algorithms, own conception computation programmes have been developed in version 7.0 Mathcad programming environment [4].

TABLE III. Components Of Electric Balance Of The Asynchronous Motor To Drive A Coal Mill

Name of	Variant I	Variant II	
the component	MIB 2-Ax 630L	MIB-X 630L 150-4	
	150-4		
Joule effect losses in	13.146	8.769	
the stator, $P_s$ [kW]			
Iron losses,	32.375	35	
$P_{Fe}$ [kW]			
Joule effect losses in	11.362	7.635	
the rotor, $P_R$ [kW]			
Mechanical and venti-	8.919	23.86	
lation losses, Pmv [kW]			
The absorbed active	1466	1475	
power, P <sub>an</sub> [kW]			
Efficiency, $\eta_n$	0.955	0.949	
The reactive power	215.101	231.947	
covering stator disper-			
sion, $Q_{\sigma s}$ [kVAr]			
The reactive power	142.793	150.081	
covering rotor disper-			
sion, $Q_{\sigma R}$ [kVAr]			
The reactive power	309.921	290.101	
needed for machine			
magnetization,			
$Q_{\mu}$ [kVAr]			
The absorbed reactive	667.816	672.129	
power, $Q_{an}$ [kVAr]			
The apparent power,	1611	1621	
S <sub>an</sub> [kVA]			
Power factor, cosp	0.91	0.91	



Fig. 5. Diagram of active powers balance at the asynchronous motor, Variant I: a - absolute values; b - percentage values.



Fig. 6. Diagram of active powers balance at the asynchronous motor, Variant II: a - absolute values; b - percentage values.



Fig. 7. Diagram of reactive powers balance at the asynchronous motor, Variant I: a - absolute values; b - percentage values.



Fig. 8. Diagram of reactive powers balance at the asynchronous motor, Variant II: a - absolute values; b - percentage values.

where in Fig. 5 and Fig. 6:

- 0 The absorbed active power,  $P_{an}$
- 1 The Joule effect losses in the stator,  $P_S$
- 2 The iron losses,  $P_{Fe}$
- 3 The Joule effect losses in the rotor,  $P_R$
- 4 The mechanical and ventilation losses,  $P_{mv}$

5 - The output power,  $P_n$ 

- while in Fig. 7 and Fig. 8:
- 0 The absorbed reactive power,  $Q_{an}$
- 1 The reactive power covering stator dispersion,  $Q_{\sigma S}$

2 - The reactive power needed for machine magnetization,  $Q_{\mu}$ 

3 - The reactive power covering rotor dispersion,  $Q_{\sigma R}$ 

The active power components have resulted according to the following computation formulas:

$$P_{s} = \frac{3R_{s}U_{s}^{2}(R_{R}^{2} + s^{2}X_{R}^{2}) \cdot 10^{-3}}{s^{2} \left[ R_{s}^{2}X_{R}^{'2} + \left(X_{s}X_{R}^{'} - X_{\mu}^{2}\right)^{2} \right] + s^{2}R_{s}R_{R}^{'}X_{\mu}^{2} + \left(R_{s}^{2} + X_{s}^{2}\right)R_{R}^{'2}}$$
[kW]
$$U^{2} \cdot 10^{-3}$$
(21)

$$P_{Fe} = 3 \frac{C_s - 10}{R_W} [kW]$$

$$P_R = \frac{R_R'}{R_s} \cdot \frac{s^2 X_{\mu}^2}{R_R'^2 + s^2 X_R'^2} P_s$$
(22)

In order to determine the mechanical and ventilation losses are used the relations from the rated regime data. Are computed with the relation (22) the Joule losses in the rotor winding ( $P_{Rn}$ ) for the rated slip ( $s_n$ ) with which are obtained:

$$P_{en} = \frac{P_{Rn}(1 - s_n)}{s_n}$$

$$P_{mv} = P_{en} - P_n$$
(23)

Therefore the total active losses will be:

$$\Delta P_n = P_{sn} + P_{Fen} + P_{Rn} + P_{mvn} \tag{24}$$

The absorbed active power and the efficiency are computed with the following relations:

$$P_{an} = P_n + \Delta P_n \tag{25}$$

$$\eta_n = \frac{P_n}{P_{an}} \tag{26}$$

The reactive power components are obtained thus:

$$Q_{\sigma s} = \frac{X_s - X_{\mu}}{R_s} P_s \tag{27}$$

$$Q_{\sigma R} = \frac{X_{R}^{'} - X_{\mu}}{X_{s} - X_{\mu}} \cdot \frac{s^{2} X_{R}^{'2}}{R_{R}^{'2} + s^{2} X_{R}^{'2}}; Q_{\sigma R} = \frac{X_{R}^{'} - X_{\mu}}{R_{R}^{'}} \cdot P_{R}$$
(28)

$$Q_{\mu} = \frac{X_{\mu} \left[ R_{R}^{'2} + s^{2} \left( X_{R}^{'} - X_{\mu} \right)^{2} \right]}{\left( X_{s} - X_{\mu} \right) \left( R_{R}^{'2} + s^{2} X_{R}^{'2} \right)} Q_{\sigma s}$$
(29)

The absorbed reactive power results:

$$Q_{an} = Q_{\sigma s} + Q_{\sigma R} + Q_{\mu} \tag{30}$$

The apparent power and the power factor result according to the relations:

$$S_a = \sqrt{P_a^2 + Q_a^2}$$

$$\cos \varphi = P_a / S_a$$
(31)

It was performed a suggestive *comparative analysis* [5], [6] of diagrams of active power balance in absolute and percentage values (obtained by reference to the absorbed active power for each constructive variants) (Fig. 9) and diagrams of reactive power balance in absolute and percentage values (obtained by reference to the absorbed reactive power for each constructive variants) (Fig. 10).



 $P\_n\_I\_II\_\%$ 

Fig. 9. Comparative diagram of active powers balance at asynchronous motor, Variant I and Variant II in percentage values.

- 0, 1 The absorbed active power, Pan
- 2, 3 The Joule effect losses in the stator,  $P_S$
- 4, 5 The iron losses,  $P_{Fe}$
- 6, 7 The Joule effect losses in the rotor,  $P_R$
- 8, 9 The mechanical and ventilation losses,  $P_{mv}$
- 10, 11 The output power,  $P_n$



 $Q\_n\_I\_II\_\%$ 

Fig. 10. Comparative diagram of reactive powers balance at asynchronous motor, Variant I and Variant II in percentage values.
 0, 1 - The absorbed reactive power, Q<sub>an</sub>

- $p_{an}$
- 2, 3 The reactive power covering stator dispersion,  $Q_{\sigma S}$

4, 5 - The reactive power needed for machine magnetization,  $Q_{\mu}$ 

6, 7 - The reactive power covering rotor dispersion,  $Q_{\sigma R}$ 

## B. Opportunity analysis of the derated motors replacement

In terms of energy, the main positive effects that are expected to replacing motors that operate in steady state derated with others having the rated power closer to those required by the driven mills are reducing power consumption and improving power factor [7], [8], [9], [10].

The results of the measurement processing of active power for the concerned regime, which were performed on five mills while operate, of the six available, were summarized in Table IV.

TABLE IV. Performed Measurements At The Mills Associated To Boiler NO. 5

Parameter	Mill no.					
	1	2	3	4	5	6
$P_{c}[kW]$	833	858	828	939	843	-
$\beta_P$	0.595	0.613	0.591	0.671	0.602	-
η	0.939	0.941	0.939	0.945	0.940	-
cosφ	0.830	0.835	0.829	0.851	0.832	-
$P_A$ [kW]	833	858	828	939	843	-
$P_a$ [kW]	782.916	807.721	777.954	888.074	792.834	-
$\Delta P [kW]$	50.083	50.278	50.045	50.925	50.165	-

TABLE V. Analysis Of The Opportunity Characteristics For The Replacement Of Derated Motors

The n	ame of	Variant I			Variant II		
charac	teristic	(used for mills			(used for mills		
		,	no. 1, 3, 5)			no. 2, 4)	
		MIE	3 2 500Y 12	20-4	MIB-V 20X 180F		
					1900-12		
Pov	wer,		800		1000		
$P_{nl}$	[kW]						
Effic	iency,		0.93		0.945		
$\eta_{nl}$							
Power	factor,	0.91		0.83			
$\cos \varphi_{nl}$							
$\beta_{PI}$		Mill no.					
		1	3	5	2	4	
		0.9786	0.9724	0.991	0.8077	0.8881	
$\Delta P_I$	[kW]	60.2151		58.2011		.011	
$P_{AI}$	[kW]	841.85	836.51	852.51	854.73	939.76	
$\delta P$	[kW]	10.13	10.17	10.05	7.922	7.275	
	[%]	16.83	16.89	16.689	13.612	12.500	
$\Delta P_{ab}$	[kW]	8.845	8.509	9.509	-3.268	0.761	
	[%]	1.051	1.017	1.115	-0.382	0.081	

where  $P_c$  [kW] represents the power consumed by the mill motor. The degree of loading with active power,  $\beta_P$  is computed with the relation (32).

$$\beta_P = P_c / P_n \tag{32}$$

The efficiency  $\eta$  and the power factor  $\cos \phi$  of steady state are computed with the relations (33), (34).

$$\eta \approx \left(\beta_P - A_\eta\right) / \left(B_\eta \cdot \beta_P\right) \tag{33}$$

$$\cos\varphi \approx \beta_P / (A_{\varphi} + B_{\varphi} \cdot \beta_P)$$
(34)

From the tables [1] are found the coefficients:  $A_{\eta}=0.0313$ ;  $B_{\eta}=1.008$ ;  $A_{\phi}=0.155$ ;  $B_{\phi}=0.944$ . The absorbed active power,  $P_A$  [kW] and the available active power to the shaft,  $P_a$  [kW] in the considered regime are determined with the relations (35), (36):

$$P_A = \beta_P \cdot P_n \tag{35}$$

$$P_a = \eta \cdot P_A \tag{36}$$

Power active losses  $\Delta P$  [kW] will be computed with the relation (37):

$$\Delta P = P_A - P_a \tag{37}$$

To analyse the opportunity of the derated motors replacement (justified because the loads are under 0.75, as can be seen from Table IV) also were used some relations for computation:

- The degree of loading with active power,  $\beta_{PI}$ :

$$\beta_{P1} = P_a / P_{n1} \tag{38}$$

- The active power losses,  $\Delta P_1$  [kW]:

$$\Delta P_1 = \left[ \left( 1 - \eta_1 \right) / \eta_1 \right] \cdot P_{n1}$$
(39)

- The absorbed active power, P<sub>A1</sub> [kW]:

$$P_{A1} = P_a / \eta_1 \tag{40}$$

- The difference between the active power losses,  $\Delta P_1$  and the power active losses,  $\Delta P$ ,  $\delta P$  in [kW] and in [%]:

$$\delta P = \Delta P_1 - \Delta P \tag{41}$$

$$\delta P_{\%} = \left( \left( \Delta P_1 - \Delta P \right) / \Delta P \right) \cdot 100 \tag{42}$$

- The difference of absorbed power in [kW] and in [%],  $\Delta P_{abs}$ :

$$\Delta P_{ab} = \Delta P_{A1} - P_A \tag{43}$$

$$\Delta P_{ab\%} = \left( \left( \Delta P_{A1} - P_A \right) / P_{A1} \right) \cdot 100$$
 (44)

The computation results have been summarized in Table V.

#### **III.** CONCLUSIONS

It was studied *the energy opportunity of the replacement of derated motors* of *the five mills which are in service*, with other motors having a rated power closer to the real load.

Thus it was found that new motors with the rated power of 800 kW (for coal mills no. 1, 3, 5) and 1000 kW (for coal mills no. 2, 4) will work in practice with rated efficiency,  $\eta_{n1}$ =0.93 and  $\eta_{n2}$ =0.945 respectively,

but this is lower than the existing motor regime efficiency ( $\eta = 0.952$ ), resulting some active power losses.

So if the motor of 1400 kW is replaced with another one at 800 kW respectively 1000 kW, instead to obtain a reduction of power losses and absorbed power it results in a growth of these.

The coal mill no. 2 is an exception at this it is found however a sensible reduction of the absorbed power (-0.382 %) as it can be seen from Table V.

Received on June 18, 2015 Editorial Approval on November 27, 2015

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